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### Midterm Exam

Course: **DS 1000A Fall 2025**

Sections: **002, 003**

Date: **Nov 2, 2025 1:00 – 3:00 pm (120 minutes)**

Instructors:

**Daniel Santaren Guerrero**

**Pavel Shuldiner**

Allowed aids: **A calculator (non-programmable, non-graphing)**



<b>Full Name</b> (e.g. Tom Marvolo Riddle):	
<b>Western ID</b> (e.g. baldemort13):	
<b>Student Number</b> (e.g. 251123456):	

1. Legibly print your Western User ID, full name, and student number in the spaces provided above.
2. The space at the top of each page is reserved for grading. **Do not write on or near the barcode.**
3. The exam has **22 pages**. The last three pages may be used for additional work space. **Clearly indicate** on the original question if you use extra pages, and label your work with the question number.
4. **Write legibly.** Illegible responses may not receive full credit. Post-exam interpretations will not be accepted. **Do not use highlighters or coloured pens as they will not be read by the scanner.**
5. Please round your answers to **2 decimal places**.

Section	Marks
Multiple Choice	25
Question 1	7
Question 2	9
Question 3	5
Question 4	13
Question 5	15
Question 6	14
Question 7	12
Total	100

## Multiple Choice

Each multiple choice question is worth 1 mark. For each question, select **one** answer only. There are no penalties for incorrect answers.

1. What is Python in the context of this course?
  - A. A large reptile, my instructor keeps one as a pet.
  - B. A high-level programming language used for data science and statistical analysis.
  - C. A British comedian from the 70's, I think his first name is Monty?
  - D. That's one of the TA's names, right?
  - E. That's the title of the DS1000 required textbook.
2. Which of the following best describes the purposes of the **pandas** library?
  - A. Data manipulation and analysis
  - B. Emotional support package for Python programmers
  - C. Data visualization
  - D. A library for storing data about bear species used in laboratory exercises
  - E. A tool for analyzing ecological datasets
3. Which of the following Python code snippets import data into a dataframe named **df** from a CSV file named **data.csv**?
  - A. `df = pd.import_csv('data.csv')`
  - B. `df = pd.load('data.csv', format='csv')`
  - C. `df = pd.read_csv('data.csv')`
  - D. `df = import('data.csv')`
  - E. `df = pd.open_csv('data.csv')`
4. A student records daily study times (in hours) over 5 days:

3   5   6   5   4

What is the median?

- A. 4.5 hours      B. 5 hours      C. 6 hours      D. 5.5 hours      E. 3 hours

5. What is the type of variable represented by the answer choices in the question below?

**How many times have you accessed social media today?**

- i. zero
- ii. once or twice
- iii. three or four times
- iv. more than four times

- A. quantitative
- B. categorical
- C. response
- D. cannot be determined from the information provided
- E. influential

6. The following four observations have mean 2:

$$x_1 = 0, \quad x_2 = 1, \quad x_3 = 2, \quad x_4 = \underline{\hspace{1cm}}$$

What must be the value of  $x_4$ ?

- A. 0                      B. 2                      C. 3                      D. 4                      E. 5

7. The following three observations have variance 0

$$x_1 = -1, \quad x_2 = -1, \quad x_3 = \underline{\hspace{1cm}}$$

What must be the value of  $x_3$ ?

- A.  $x_3 = 2$               B.  $x_3 = 0$               C.  $x_3 = 1$               D.  $x_3 = -1$               E.  $x_3 = -3$

8. Which of the following statements is **false**?

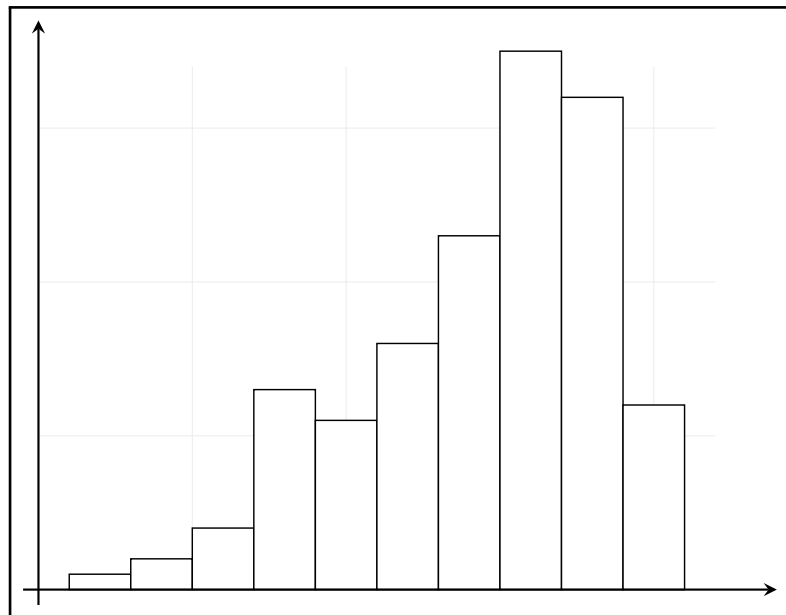
- A. The interquartile range (IQR) is a measure of spread that is resistant to outliers.
- B. The response variable is plotted on the  $x$ -axis in a scatterplot.
- C. The correlation coefficient  $r$  measures the strength and direction of a linear relationship between two quantitative variables.
- D. The normal distribution  $N(0, 1)$  has mean 0 with standard deviation 1.
- E. Correlation does not imply causation.

9. A sociologist surveyed first-year undergraduates about their daily study hours and nightly sleep hours. The table below summarizes the results.

Hours Studied	Hours Slept			
	Less than 6	6 to 8	More than 8	Total
Less than 2	20	40	20	80
2 to 3	10	30	10	50
3 to 4	20	20	20	60
More than 4	20	20	10	50
<b>Total</b>	70	110	60	240

What proportion of the students slept less than 6 hours at night?

- A. 0.29  
 B. 0.3  
 C. 0.25  
 D. 0.33  
 E. Impossible to deduce from the information provided
10. In Naples, Florida, most houses are priced between \$200,000 and \$500,000, but a few waterfront properties cost up to \$150 million. The distribution of house prices is best described as
- A. symmetric      B. normal      C. resistant      D. left skewed      E. right skewed
11. Which of the following statements best describes the histogram below?



- A. It is left-skewed.  
 B. It is approximately symmetric.  
 C. It is right-skewed.  
 D. There are several outliers.  
 E. It appears to be from a normal distribution.

12. Which statement about correlation is correct?
- A. Changing the units of measurement does not change the correlation.
  - B. A correlation of  $-0.9$  indicates weak association between variables.
  - C. Correlation values range from 0 to 1.
  - D. It depends on which variable is the explanatory variable ( $x$ ) and which is the response variable ( $y$ ).
  - E. If the correlation is 0, then there is no relationship between the two variables.
13. A researcher studying plant growth calculates the regression equation:  $\text{height} = 2.5 + 0.8x$ , where  $x$  is days of sunlight exposure. What can we conclude about the correlation between height and sunlight exposure?
- A.  $r$  is positive, but the exact value cannot be determined from this information.
  - B.  $r$  is negative, but the exact value cannot be determined from this information.
  - C.  $r = 0.8$
  - D.  $r = \frac{1}{0.8}$
  - E.  $r = 2.5$
14. What does `np.random.seed(42)` do?
- A. Generates 42 random numbers and stores them in memory for faster access
  - B. Limits all random values to be between 0 and 42
  - C. Sets the random seed to 42, ensuring reproducible random number generation
  - D. Creates a random array with 42 elements as the default size
  - E. Sets 42 as the starting value for all random number sequences
15. Which of the following outputs is printed by the following Python code snippet?

```
heights = [75, 64.5, 67, 89, 70.4, 63, 50.9]
print(heights[2:4])
```

- A. `[67, 89]`      B. `[67, 89, 70.4]`      C. `67, 89`      D. `70.4, 63, 50.9`      E. `IndexError`

16. Which statement about density curves is **false**?

- A. Density curves never fall below the horizontal axis.
- B. The area under the curve between two values represents the proportion of observations in that interval.
- C. The total area under any density curve depends on the curve's shape.
- D. Density curves represent an idealized model of a distribution.
- E. The median divides the area under the curve in half.

17. What is the coefficient of determination for the linear regression model obtained based on the following Python code snippet and its output?

```
model_modified = stats.linregress(x = possum_modified['age'], y = possum_modified['headL'])
model_modified.intercept
model_modified.slope
model_modified.rvalue
```

90.72

0.36

0.26

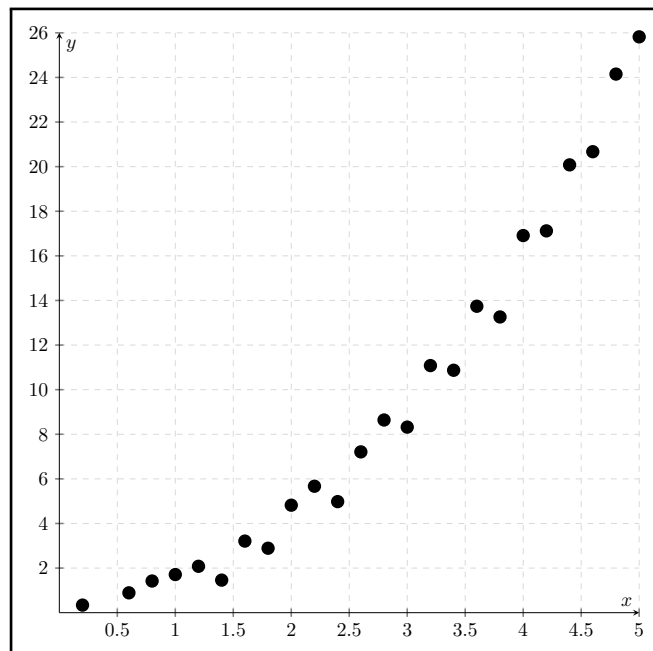
- A. 0.9072      B. 0.36      C. 0.26      D. 0.13      E. 0.07

18. In the following stemplot, stems are whole percentages and leaves are tenths. Which of the following statements is true?

- A. The distribution is right-skewed
- B. 16.8 is an outlier
- C. The mean is approximately 11.1
- D. The mode is 12.3
- E. 4.2 is an outlier

4	2
5	
6	
7	
8	
9	7 9
10	0 8
11	1 5 5 6 6
12	0 1 2 2 2 3 4 4 4 4 5 7 8 8 8 9 9 9
13	0 1 2 3 3 3 3 3 4 4 4 8 9 9
14	0 2 6 6 6
15	2 3
16	8

19. Suppose we have a variable  $X$  that follows a standard Normal distribution. Which of the following best approximates the proportion of values of  $X$  have  $z$ -scores between 0 and 2?
- A. 68%                      B. 50%                      C. 99.7%                      D. 95%                      E. 47.7%
20. A least-squares regression line has slope 450. After removing one data point and the least-squares regression line, the new slope is -10,000. The removed point is best described as
- A. influential  
B. resistant  
C. low leverage point  
D. lowkey based  
E. an outlier in only the  $y$ -direction
21. A variable has the following five-number summary: 0, 10, 20, 30, 70. How many potential outliers does this variable contain?
- A. At least one      B. 1                      C. 0                      D. 2                      E. 3
22. Which of the following best describe the direction, form and strength of the relationship in the scatterplot below?



- A. positive, linear, strong  
B. negative, linear, strong  
C. positive, non-linear, strong  
D. negative, non-linear, strong  
E. no relationship

23. Suppose it was found that the least-squares regression line predicting house price ( $y$ ) from size in square feet ( $x$ ) is given by

$$\hat{y} = 20000 + 150x$$

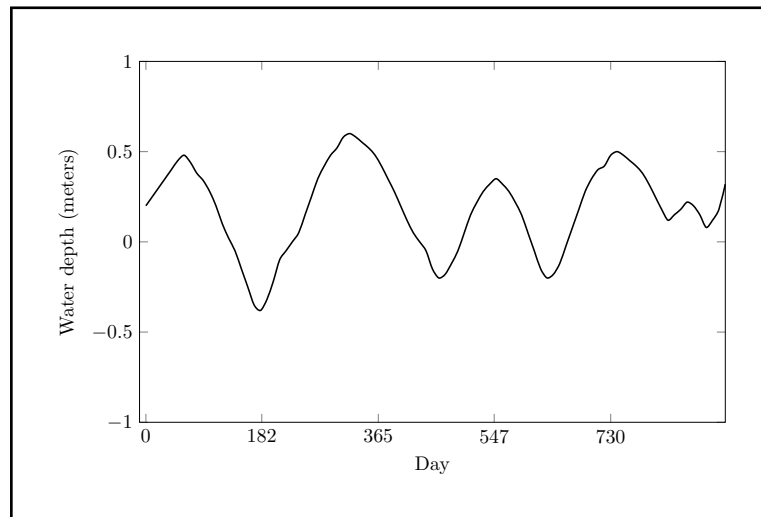
Which of the following provides the correct interpretation regarding the slope of the regression line?

- A. As house size increases by 1 square foot, the expected (or average) increase in house price is \$150.
  - B. As house size increases by 150 square feet, the expected (or average) increase in house price is \$20,000.
  - C. As house size increases by 20,000 square feet, the expected (or average) increase in house price is \$150.
  - D. As house size increases by 1 square foot, the expected (or average) increase in house price is \$20,000.
  - E. As house price increases by \$1, the expected (or average) increase in house size is 150 square feet.
24. Continuing from question 23: Which of the following gives the least-squares regression line predicting square footage ( $y$ ) based on house price ( $x$ )?

- A. The line cannot be determined from the information provided.
- B.  $\hat{y} = -133.33 + 0.0067x$
- C.  $\hat{y} = 20000 + 150x$
- D.  $\hat{y} = -20000 + 150x$
- E.  $\hat{y} = 20000 + \frac{1}{150}x$

25. The following time plot shows the water depth (in meters) measured in a well over a period of three years. Which of the following statements best describes what we can infer from the plot?

- A. The water depth trends downwards.
- B. The water depth trends upwards.
- C. The water depth shows a seasonal pattern with no overall trend.
- D. The water depth fluctuates randomly with no discernible pattern.
- E. A linear model of water depth over time would be a good fit.





## Short Answer

### Question 1 (7 marks)

A random sample of 7 graduate students tracked their weekly coffee consumption (in cups), and their results are as follows:

3	6	6	7	10	10	10
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- (a) (2 marks) What is/are the mode(s) of weekly coffee consumption of graduate students?

Final answer:

- (b) (5 marks) Determine the five-number summary for the students' weekly coffee consumption.

Final answer:

## Question 2 (9 marks)

A random sample of 3 undergraduate students tracked their average daily hours of sleep, and the results are as follows:

2	4	6
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- (a) (1 mark) What kind of variable is the average daily hours of sleep? You do not have to justify your answer.

Final answer:

- (b) (1 mark) What are the individuals described by this dataset? You do not have to justify your answer.

Final answer:

- (c) (2 marks) List two suitable visualizations for this variable type. You do not have to justify your answer.

Final answer:

- (d) (1 mark) Describe the shape of this distribution. You do not have to draw or justify your answer.

Final answer:

- (e) (4 marks) Find the sample mean and standard deviation for the undergraduate students' average daily hours of sleep.

Final answer:

### Question 3 (5 marks)

The variable  $x$  has the following observations:

5	10	10	10	11	12	12	13
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It is known that the quartile values of  $x$  are

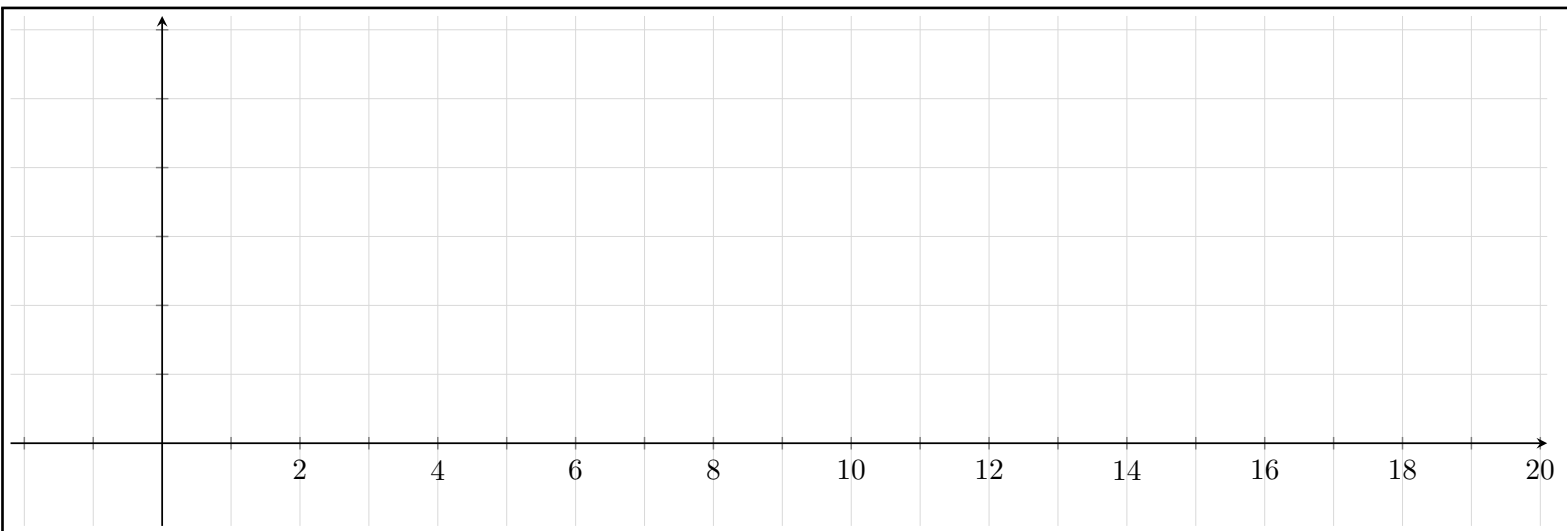
$$Q_1 = 10, \quad Q_2 = 10.5, \quad Q_3 = 12$$

(You may use these values to answer the following questions without recalculating them.)

- (a) (2 marks) Compute the interquartile range for this variable.

Final answer:

- (b) (3 marks) Draw a modified boxplot of this data.



#### Question 4 (13 marks)

The first two Starbucks cafes which opened in Canada are located in Vancouver and Toronto. The ratings of nearby cafes were collected and it was found that cafe ratings are **normally distributed** in both cities.

In Vancouver, the average cafe rating is 3.8 with a standard deviation of 0.2, while in Toronto, the average cafe rating is 4.1 with a standard deviation of 0.3. The first Vancouver Starbucks cafe has a rating of 4.2, while the first Toronto Starbucks cafe has a rating of 4.4.

City	First Starbucks Rating	City Mean ( $\mu$ )	City SD ( $\sigma$ )
Vancouver	4.2	3.8	0.2
Toronto	4.4	4.1	0.3

- (a) (4 marks) What proportion of Vancouver cafes have ratings at or below the first Vancouver Starbucks cafe's rating of 4.2?

Final answer:

- (b) (3 marks) Suppose that the first Toronto Starbucks cafe ranks at the 84th percentile among Toronto cafes. Based on part (a), which cafe's rating is higher relative to its city? Briefly explain.

(c) (4 marks) What proportion of cafes in Vancouver have ratings between 3.4 and 4.2?

Final answer:

(d) (2 marks) What is the probability that a randomly selected cafe in Vancouver has a rating exactly equal to 4.1?

Final answer:

### Question 5 (15 marks)

A study tracked 1000 days at an ice cream shop to examine the relationship between daily temperature ( $x$  in  $^{\circ}\text{C}$ ) and daily ice cream sales ( $y$ , in cones sold).

$$r = 0.8, \quad \bar{x} = 20^{\circ}\text{C}, \quad s_x = 5^{\circ}\text{C}, \quad \bar{y} = 150 \text{ cones}, \quad s_y = 25 \text{ cones}$$

- (a) (2 marks) What is the proportion of variation in ice cream sales which is explained by the least-squares regression on the daily temperature?

Final answer:

- (b) (3 marks) What are the slope and the intercept of the least-squares regression line?

Final answer:

- (c) (2 marks) Write down the least-squares regression line using the coefficients you found in part (b).

Final answer:

(d) (4 marks) What are the predicted ice cream sales when the daily temperature is  $60^{\circ}\text{C}$ , using the regression line you found in part (b)? Is there a problem with this prediction? Briefly explain.

(e) (4 marks) Suppose the regression line is  $\hat{y} = 100 + 10x$ . If  $(x, y) = (10, 100)$  is a data point in the dataset, what would be its residual?

Final answer:

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### Question 6 (14 marks)

A university is comparing two tutors (Tutor A and Tutor B) to determine which is more effective at helping students pass their exams. Data was collected from 80 students across beginner-level and advanced-level courses. Their combined results are summarized in the table below.

Result	Tutor A	Tutor B	Total
Fail	18	8	26
Pass	42	12	54
<b>Total</b>	60	20	80

- (a) (1 mark) Find the probability that a student was tutored by Tutor A given that they failed.

Final answer:

- (b) (2 marks) Find the odds of passing for students tutored by Tutor A.

Final answer:

- (c) (3 marks) Calculate the pass rate (as a proportion) for each tutor. Based on the combined data, which tutor is more effective?

Final answer:



When the data is separated by course level, the results are as shown in the tables below.

Beginner Level				Advanced Level			
Result	Tutor A	Tutor B	Total	Result	Tutor A	Tutor B	Total
Fail	10	1	11	Fail	8	7	15
Pass	40	9	49	Pass	2	3	5
Total	50	10	60	Total	10	10	20

- (d) (6 marks) Calculate the pass rate (as a proportion) for each tutor at each course level.  
Which tutor is more effective for beginner-level courses? Which is more effective for advanced-level courses?

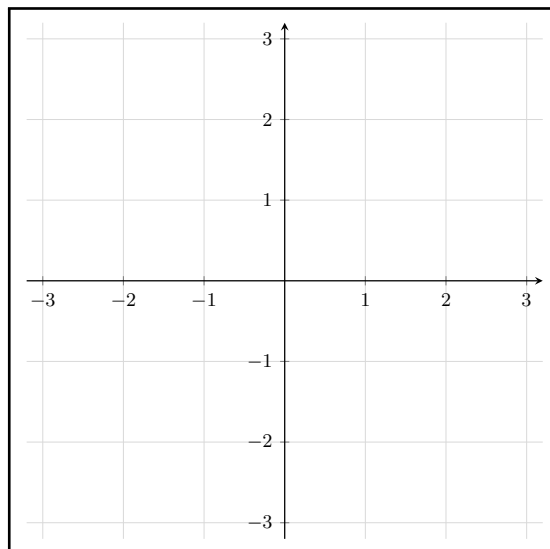
- (e) (2 marks) What statistical phenomenon explains why the better tutor in part (c) differs from the better tutor at each individual course level in part (d)?

Final answer:

**Question 7 (12 marks)**

(a) (3 marks) Plot the following data on the scatterplot provided.

$x$	$y$
-1	-2
0	0
1	2



(b) (5 marks) Find the correlation of  $x$  and  $y$ . Be sure to justify your answer.

Final answer:

(c) (2 marks) Find the correlation of  $y$  and  $x$ . Be sure to justify your answer.

$y$	$x$
$-2$	$-1$
$0$	$0$
$2$	$1$

Final answer:

(d) (2 marks) Find the correlation of  $x$  and  $z$ , where  $z = 2y + 1$ . Be sure to justify your answer.

$x$	$z$
$-1$	$-3$
$0$	$1$
$1$	$5$

Final answer:

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# Scratch Work

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